

MATH 19 MAKEUP MIDTERM I
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BROWN UNIVERSITY
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1 Find $\int \frac{\sqrt{x^2 + 16}}{x^4} dx$.

2 Find the arc length of the portion of the graph of

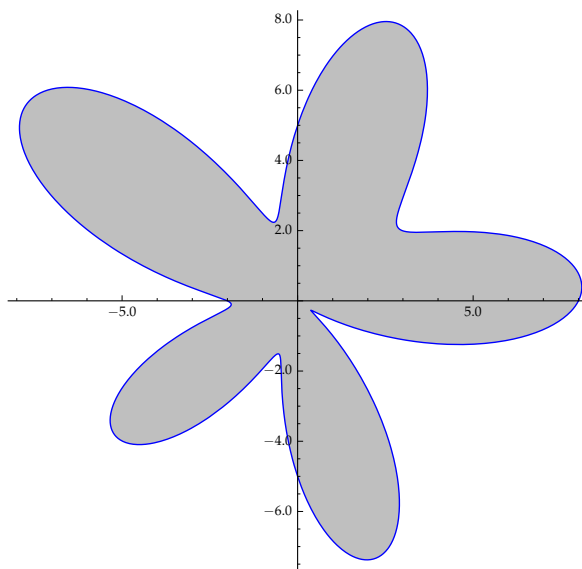
$$f(x) = 2\sqrt{e^x - 1} - 2 \arctan(\sqrt{e^x - 1})$$

which lies between the vertical lines $x = 0$ and $x = \ln 4$. Express your answer as an integer.

3 Find the area of the region below, where the curve is the graph of the polar equation

$$r = 5 + \sin(x) + \sin(3x) + 3 \cos(3x).$$

(Note: you have some tricks up your sleeve for calculating the integral you need to calculate—you do not have to do it all out by hand.)



4 How much work does it take to move an object in the presence of a force $F(x) = \sqrt{x}$ from the location $x = 0$ to the location $x = 1$?

5 Find complex numbers z and w such that

$$\begin{aligned}2z + (3 + i)w &= 3 + i \\ z + 2w &= 2 + i.\end{aligned}$$

6 Find f such that $f''(x) + 3f'(x) + 2f(x) = 0$ and $f(0) = 5$ and $f'(0) = -5$.